Reducing communications on a dense Cholesky factorization

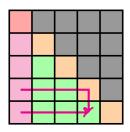
Collin Jean-Alexandre

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Contexte

- Computer science department of the university of Bordeaux
- 2 Topal's team with Olivier Beaumont, Lionel Eyraud-Dubois and Mathieu Vérité
- Internship: Creation of data allocation and scheduling strategies.

Cholesky Factorization



Point to point communications

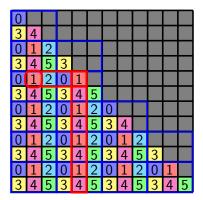
$$Ax = b$$
 and $A = LL^T$

$$\forall i, j \in \{1 \dots S\} \ \forall k \in \{1 \dots P\} x_{i,j}^k \in \{0; 1\}$$

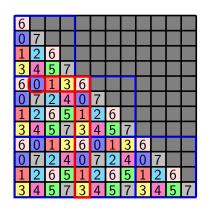
 $\forall i \in \{1 \dots S\} \ \forall k \in \{1 \dots P\} y_i^k \in \{0; 1\}$

State of the art: 2DBC and SBC





6 0 1 3 0 7 2 4 1 2 6 5 3 4 5 7



2DBC



Pattern research with a linear problem solver

- Description of the problem with constraints
- Using CPLEX to solve the problem

Constraints

$$\left\{ \begin{array}{ll} (1) & \forall i,j \in \{1 \ldots S\} \\ & \sum\limits_{k \in \{1 \ldots P\}} x_{i,j}^k = 1 \\ \\ (2) & \forall i,j \in \{1 \ldots S\} \ \forall k \in \{1 \ldots P\} \\ & X_{i,j}^k \leqslant y_i^k \\ \\ (3) & \forall k \in \{1 \ldots P\} \\ & m \leqslant \sum\limits_{i,j \in \{1 \ldots S\}} x_{i,j}^k \leqslant M \quad \text{load distribution} \\ \\ (4) & \forall i \in \{1 \ldots S\} \\ & \sum\limits_{k \in \{1 \ldots P\}} y_i^k \leqslant \alpha \qquad \text{communication} \\ \end{array} \right.$$

Pattern research with a greedy algorithm

Trying to find another method more time-efficient. An algorithm on two steps:

- For every node, find the tiles where it's the more efficient
- Using a coupling algorithm to find what are the best tiles for every nodes

What's next?

After obtaining results from the two methods I will test them on plafrim to see if the time and communications are reduced.