

The logo for Inria, featuring the word "Inria" in a white, elegant cursive script font, set against a solid red rectangular background.

# PaStiX: Distributed Interface

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# Summary

01. PaStiX
02. Degree of Freedom
03. From *CSC* to *Block CSC*
04. MPI implementation
05. Conclusion

# 01

PaStiX

### PaStiX = Parallel Sparse Linear Algebra Solver

- Linear Algebra Solver
  - > Solves  $Ax = b$
- Sparse
  - > Matrix with a lot of zero elements
- Parallel
  - > Several schedulers:
    - Sequential
    - Static
    - Dynamic
    - StarPU
    - Parsec
  - > MPI

### 4 steps

- Analyse
  - > Ordering: Scotch, Metis
    - Computes the permutation  $P$
  - > Symbolic Factorisation
    - Computes the graph of  $A$
  - > Blend
    - Computes the blocks Partition of  $A$
- Numerical Factorisation
  - > Computes  $PAP^T$
  - > Stores  $PAP^T$  in blocks
- Solve
  - > Solves  $PAP^T P x = P b$
- Refinement
  - > Refines the solution  $x$

## Analyse

- Computes the permutation  $P$
- Computes the graph of  $A$
- Computes the blocks Partition of  $A$

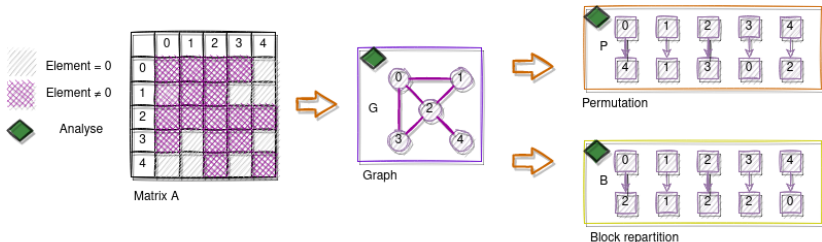


Figure: Example of the analyse step for a matrix  $A$

## Factorisation

- Computes the permutation  $PAP^T$
- Stores  $PAP^T$  in the blocks

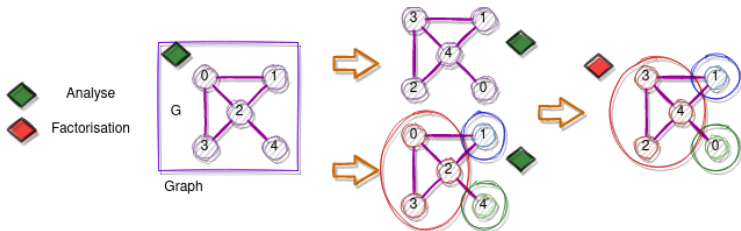


Figure: Example of the factorisation step for a matrix  $A$ : the graphs

## Factorisation

- Computes the permutation  $PAP^T$
- Stores  $PAP^T$  in the blocks

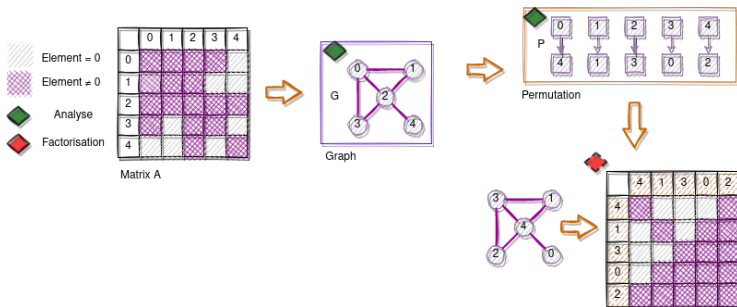


Figure: Example of the factorisation step for a matrix  $A$ : permutation



## Factorisation

- Computes the permutation  $PAP^T$
- Stores  $PAP^T$  in the blocks

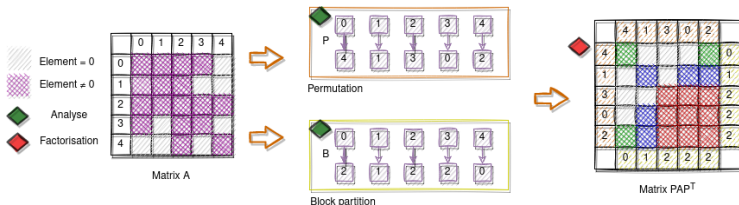


Figure: Example of the factorisation step for a matrix  $A$

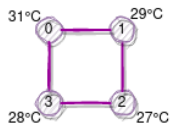
# 02

## Degree of Freedom

## Single DoF: temperature

	0	1	2	3
0	31	...	...	...
1	...	29	...	...
2	0	...	27	...
3	...	0	...	28

Matrix A



Graph

Figure: Graph of a matrix A with Single DoF

## Multiple Constant DoF: temperature and pressure

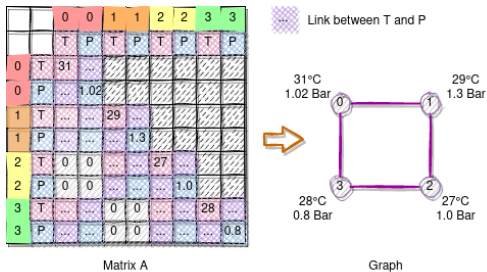


Figure: Graph of a matrix A with Multiple Constant DoF

## Multiple Variadic DoF: temperature, pressure and volume

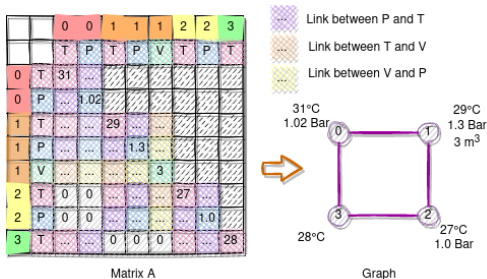


Figure: Graph of a matrix A with Multiple Variadic DoF

# 03

From *CSC* to *Block CSC*

## CSC format

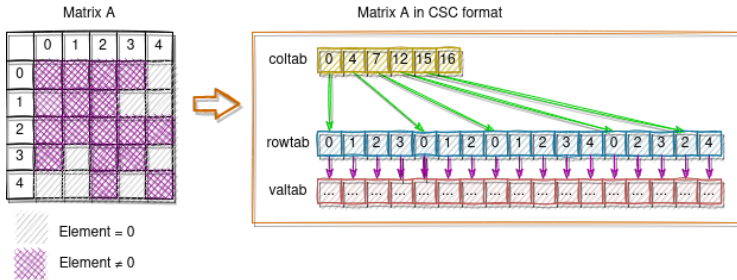
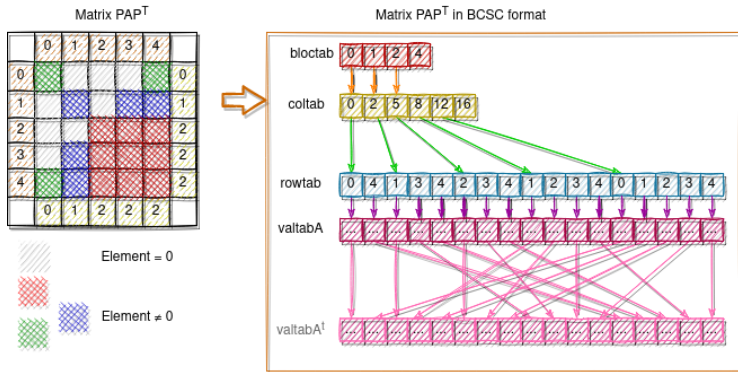
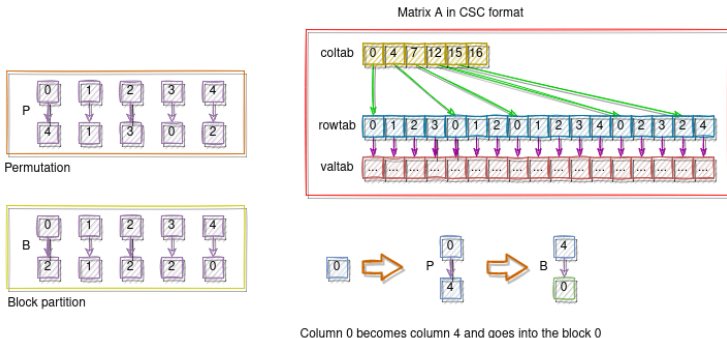


Figure: A in CSC format

**BCSC format**Figure:  $PAP^T$  in BCSC format



## Shared memory implementation

Figure: CSC to  $BCSC$  in shared memory

# 04

## MPI implementation

## Matrix distributed in memory

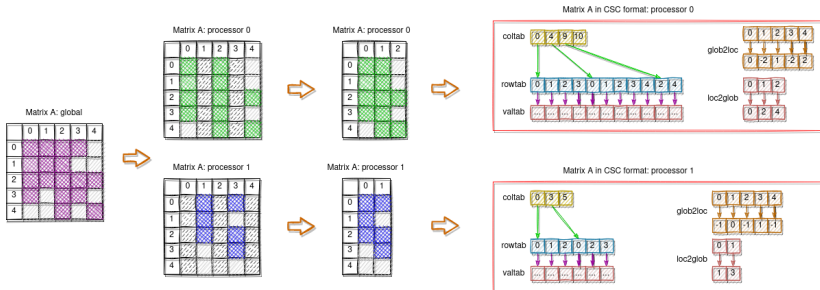


Figure: Matrix Partition in distributed memory

## Block distributed in memory

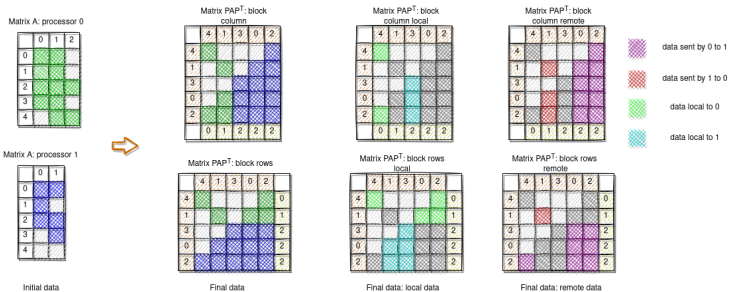


Figure: Block Partition in distributed memory

## Distributed memory implementation

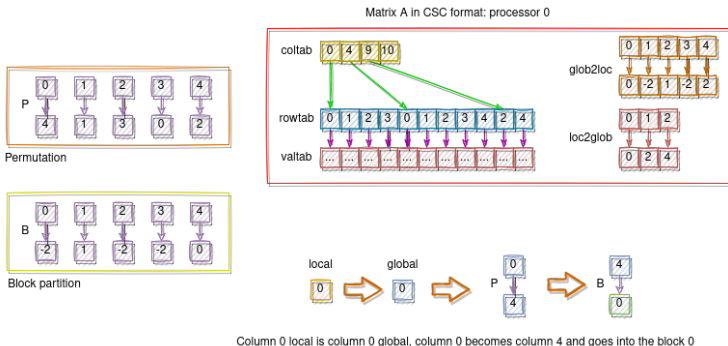
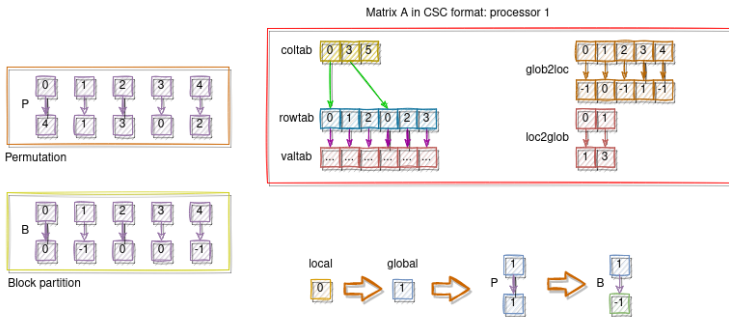


Figure: CSC to BCSC in distributed memory: processor 0

## Distributed memory implementation



Column 0 local is column 1 global, column 1 becomes column 1 and goes into a block of processor 0

Figure: CSC to BCSC in distributed memory: processor 1

### Data buffers

- Sending indexes:  $nbr_{proc} - 1$
- Sending values:  $nbr_{proc} - 1$
- Receiving indexes: 1
- Receiving values: 1

### Count the data

- If *DoF* equals to 1: 1 value per 2 indexes.
- If *DoF constant* equal to  $d$ :  $d$  per 2 indexes.
- If *DoF variadic*: number of values per 2 indexes depends on the *DoF* of the indexes.

# 05

## Conclusion



### Next steps

- Reduce the amount of data exchanged
- Distributed Solve and Refinement:
  - > Exchange the data for the vector
  - > TRSM part of the solve
- Variadic degree of freedom